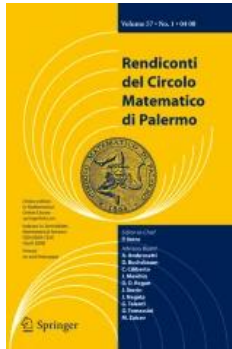# Eigenfunction expansion for impulsive singular Hahn–Dirac system

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## Abstract

In this study, a singular impulsive Hahn–Dirac system is studied. A spectral function has been established for this type of system. With the help of this function, the Parseval equation and eigenfunction expansion were obtained.

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